There is no need to start each question in this section on a fresh page. Geometry theorems need not be referred to when used.

1. Find the value of x in Figure 1.

(4 marks)

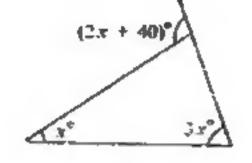


Figure 1

2. Factorize

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- (a) a(3b-c)+c-3b
- $(h)^{-} x^{+} 1$ .

(5 marks)

3. What is the product of the roots of the quadratic equation  $2x^2 + kx - 5 = 0$ ? If one of the roots is 5, find the other root and the value of k.

(5 marks)

4. If  $0^{\circ} < \theta < 360^{\circ}$  and  $\sin \theta = \cos 120^{\circ}$ , find  $\theta$ .

(5 marks)

5. In Figure 2, AB is a vertical thin rod. It is retailed about A to position AB' such that LBAB' = 30°. If B' is 50 mm higher than B. find the length of the rod, correct to 3

significant figures. (5 marks)

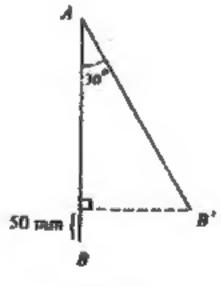


Figure 2

6. At a fun fair, each mother there had brought 2 children along. At the end of the day, it was found that 36 mothers had lost one or both of their children and 62 children had lost their mothers. How many mothers lost only one of their children and how many mothers lost both of their children?

(5 anucka)

7. Given that  $a(1+\frac{x}{100})=b(1-\frac{x}{100})$ , express x in terms of a and b.

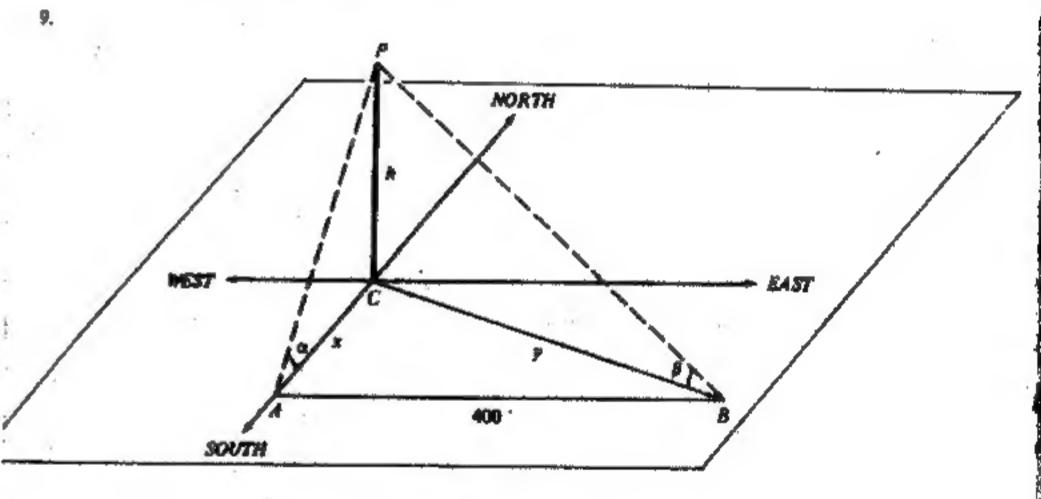
(5 marks)

8. A factory employs 10 skilled, 20 semi-skilled, and 30 similar workers. The daily wager per worker of the three kinds are in the ratio 4:3:2. If a skilled worker is paid \$120 a day, find the mean daily stage for the 60 workers.

(5 marks)

SECTION D

Assert SDS questions in this section. Each question carries 10 punks.



Pigare 3

In Figure 3, PC represents a vertical object of height h metres. From a point A, south of C, the angle of elevation of P is n. From a point B, 400 metres cust of A, the angle of elevation of P is  $\beta$ . AC and BC are x metres and y metres respectively.

- (a) (ii) Express x in terms of h unit at,
  - (ii) Express y in terms of h and \$.

(4 marks)

(b) If  $\alpha = 60^\circ$  and  $\beta = 30^\circ$ , find the value of h correct to 3 significant figures.

(6 marks)

Amwer ALL questions in this section.

There is no need to start each question in this section on a fresh page. Geometry theorems used not be referred to when used.

1. Find the value of at in Figure 1.

(4 marks)

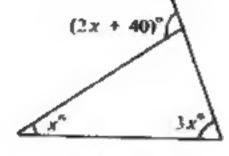


Figure 1

2. Factorize

(a) 
$$a(3b-c)+c-3b$$
,

(b) 
$$x^4 - 1$$
.

(5 marks)

3. What is the product of the roots of the quadratic equation  $2x^2 + kx - 5 = 0$ ? If one of the roots is 5, find the other root and the value of k.

(5 marks)

4. If  $0^{\circ} < \theta < 360^{\circ}$  and  $\sin \theta = \cos 120^{\circ}$ , find  $\theta$ .

(5 marks)

5. In Figure 2. AB is a vertical thin rnd. It is rotated about A to position AB' such that  $\angle BAB' = 30^\circ$ . If B' is 50 mm higher than B. find the length of the rod, correct to 3 significant figures.

(5 marks)

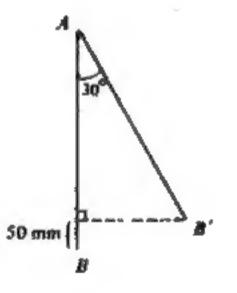


Figure 2

6. At it fun fair, each mother there had brought 2 children along. At the end of the day, it was found that 36 mothers had lost one or both of their children and 62 children had lost their mothers. How many mothers just only one of their children and how many mothers just both of their children?

(S marks)

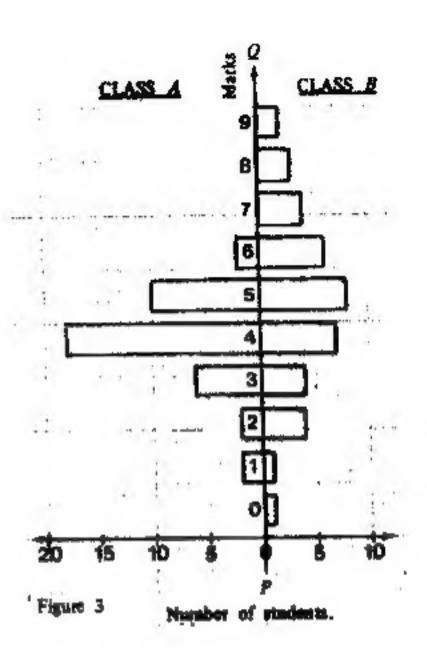
7. Find x if  $\log_3(x-3) + \log_3(x+3) = 3$ .

(5 marka)

Two classes. A and B, each of 40 students, took a test. In the test, students may score 0, 1, 2, 3, 4, 5, 6, 7, 8 or 9 marks. In Figure 3, the distribution of marks of class A is shown in the bar chart on the left of PQ and that of class B is shown on the right.

- (a) Find, by inspection, which class has a greater standard deviation of marks.
- (b) If 70 students from the two classes
  pass the test, what is the minimum
  mark that a student should get in
  order to obtain a pass?

  (5 marks)



SECTION B. Asswer SIX questions in this section.

Each question carries 10 marks.

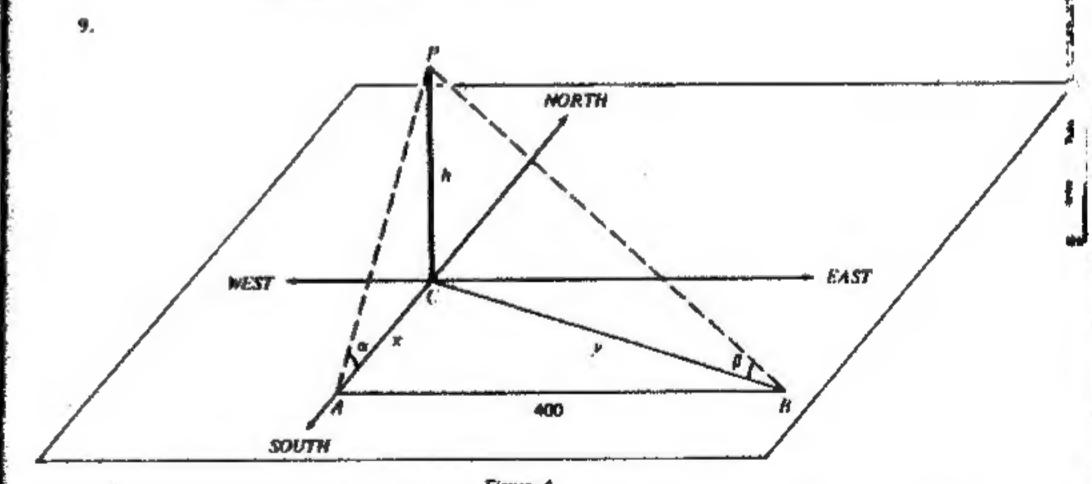


Figure 4

In Figure 4, PC represents a vertical object of height h metres. From a point A, south of C, the angle of elevation of P is  $\alpha$ . From a point B, 400 metres east of A, the angle of elevation of P is  $\beta$ . AC and BC are x metres and y metres respectively.

- (a) (i) Express x in terms of h and a.
  - (ii) Express y in terms of h and f.

(4 marks)

) If  $\alpha = 60^{\circ}$  and  $\beta = 30^{\circ}$ , find the value of h correct to 3 significant figures.

(6 marks)

C.E. MATH. I (SYL. 3) (E)

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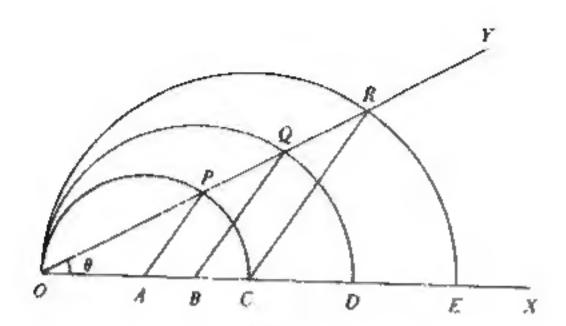


Figure 4

A, B and C are three points on the line OX such that OA = 2, OB = 3 and OC = 4. With A, B, C as centres and OA, OB, OC as radii, three semi-circles are drawn as shown in Figure 4. A line OY cuts the three semi-circles at P, Q, R respectively.

- If  $\angle YOX = \theta$ , express  $\angle PAX$ ,  $\angle QBX$  and  $\angle RCX$  in terms of  $\theta$ .
- Find the following ratios: area of sector OAP; area of sector OBQ : area of sector OCR.
- If RD1OX, calculate the angle #.

Let k > 0.

- (n) Find the common ratio of the geometric progression k, 10k, 100k.
  - Find the sum of the first it terms of the geometric progression k, 10 k, 100 k, ....
- (b) (i) Show that log 10 k, log 10 lok, log 10 100 k is an arithmetic progression.
  - Find the sum of the first in terms of the arithmetic progression log 10 k, log 10 k, log 10 f 00 k, .... Also, if n = 10, what is the sum?

Total Marks Candidate Number Centre Number Seat Number on this page

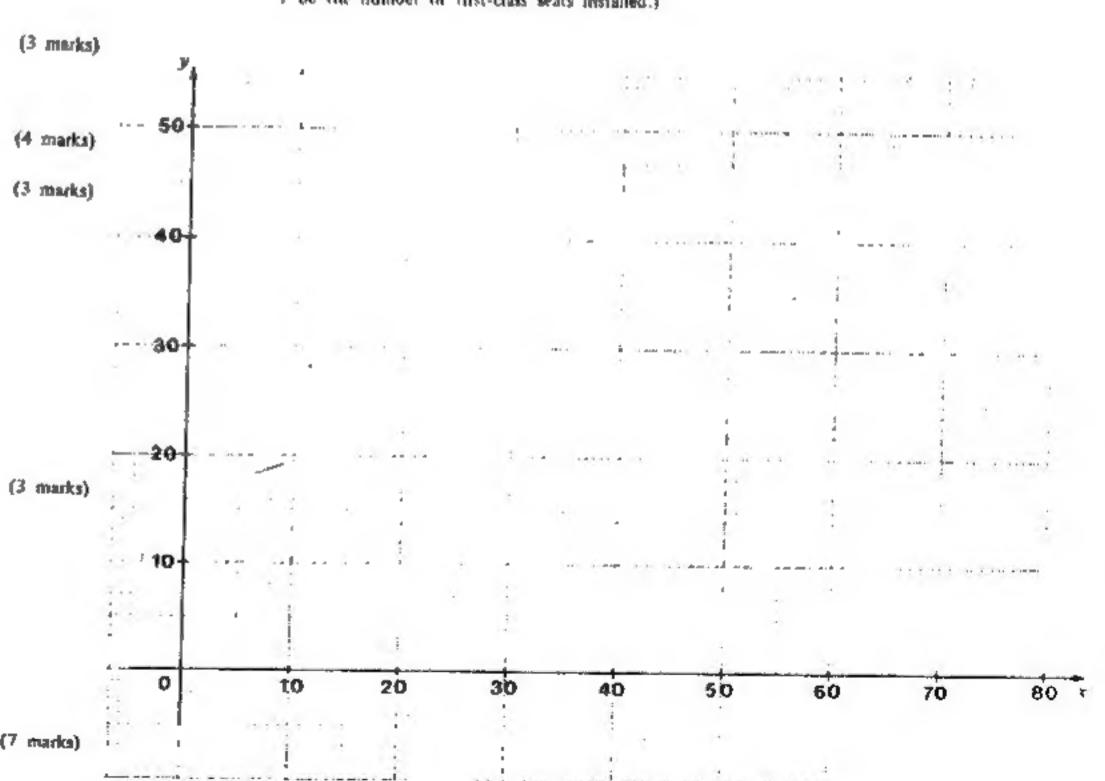
12. If you attempt this question, fill in the details in the first three hoxes above and tie this sheet into your answer book.

An airline company has a small passenger plane with a luggage capacity of 720 kg, and a floor area of 60 m2 for installing passenger seats. An economy-class sent takes up 4 m2 of floor area while a first-class seat takes up 1.5 m<sup>2</sup>. The company requires that the number of first-class seats should not exceed the number of economy-class seats. An economy-class passenger cannot carry more than 10 kg of luggage while a first-class passenger cannot carry more than 30 kg of

The profit from selling a first-class ticket is double that from selling an economy-class ticket. If all tickets are sold out in every flight, find graphically how many economy-class seats and how many first-class seats should be installed to give the company the maximum profit.

(10 marks)

(Let x be the number of economy-class seats installed, P be the number of first-class seats installed.)



(7 made)

C.E. MATHS: [ (F)

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$$\vec{OA} = \vec{3i} + \vec{4j},$$

$$\overrightarrow{OP} = x\overrightarrow{i} + y\overrightarrow{j}.$$

O is the origin,  $\vec{i}$  and  $\vec{j}$  are perpendicular unit vectors as shown in Figure 5.

- (a) (i) Evaluate  $(3\vec{i} + 4\vec{j}) \cdot (x\vec{i} + y\vec{i})$ .
  - (ii) Find  $|\vec{OA}|$  and  $|\vec{OP}|$ .
  - (iii) Hence, express cos LAOP in terms of x and y

(4 marks)

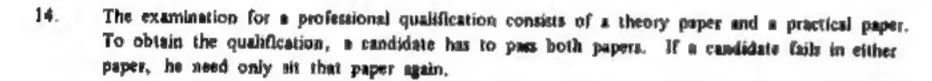
Figure 5

(b) Express cos LBOP in terms of x and y.

(3 marks)

(c) Using the results of (a) and (b), find the equation of the internal bisector of LAOB.

(3 marks)



The probabilities of passing the theory paper for two candidates A and B are both  $\frac{9}{10}$  and their probabilities of passing the practical paper are both  $\frac{2}{3}$ . Find the probabilities of the following events:

- (a) Candidate A obtaining the qualification by sitting each paper only once.

  (3 marks)
- (b) Candidate A failing in one of the two papers but obtaining the qualification with one re-examination.
- (c) At least one of the candidates A and B obtaining the qualification without any re-examination.

(3 marks)

15. The circle

Kin or

$$x^2 + y^2 - 10x + 8y + 16 = 0$$

the y-axis at A and B and touches the y-axis at T as shown in Figure 6.

- (a) Find the coordinates of A, B and T. (5 marks)
- (b) C is a point on the circle such that AC | TB.
  - (i) Find the equation of AC.

Figure 6

(ii) Find the coordinates of C by solving simultaneously the equation of AC and the equation of the given circle.

(5 marks)

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16. If you attempt this question, fill in the details in the first three boxes above and tie this sheet into your answer book.

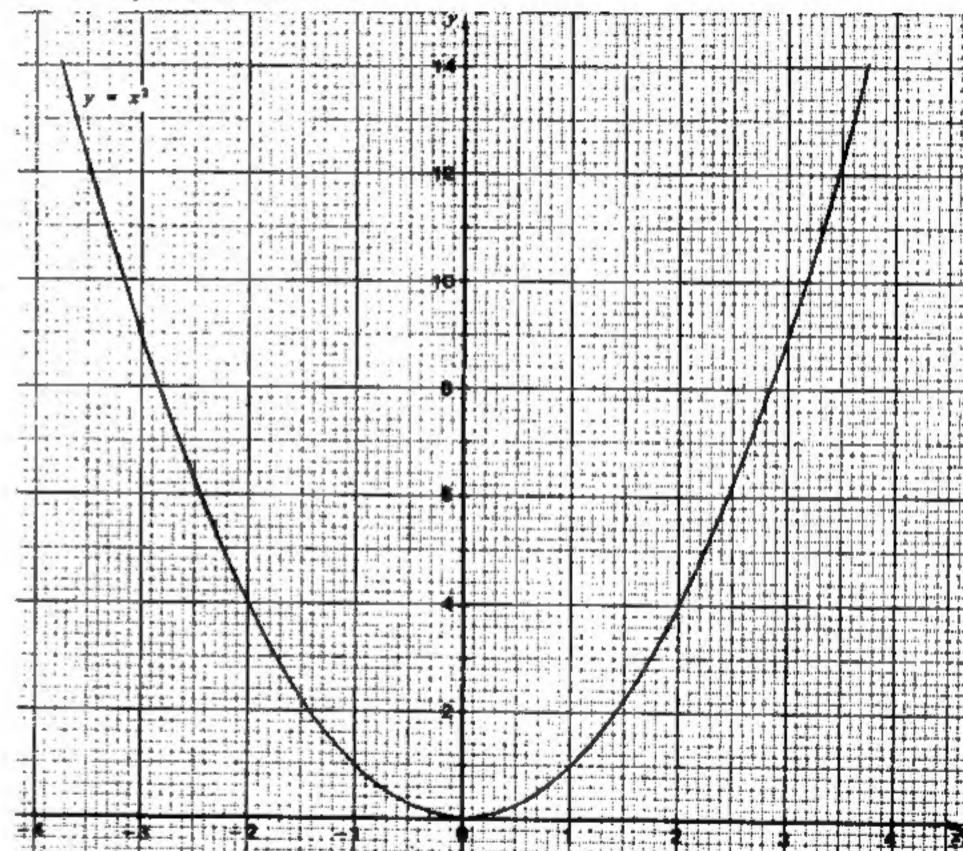


Figure 7

Figure 7 shows the graph of  $y=x^2$ . By drawing suitable lines in the same figure, solve the following:

(a) 
$$x^2 - 2x - 5 = 0$$
,

(4 marks)

(b) 
$$x^2-2x-5>0$$
,

(2 marks)

(c) 
$$2x^2 - 2x - 5 = 0$$

(4 marks)

(Answers should be correct to I decimal place. All straight lines should be labelled.)

Candidate Number	Centre Number	Seat Number	Total Marks on this page	

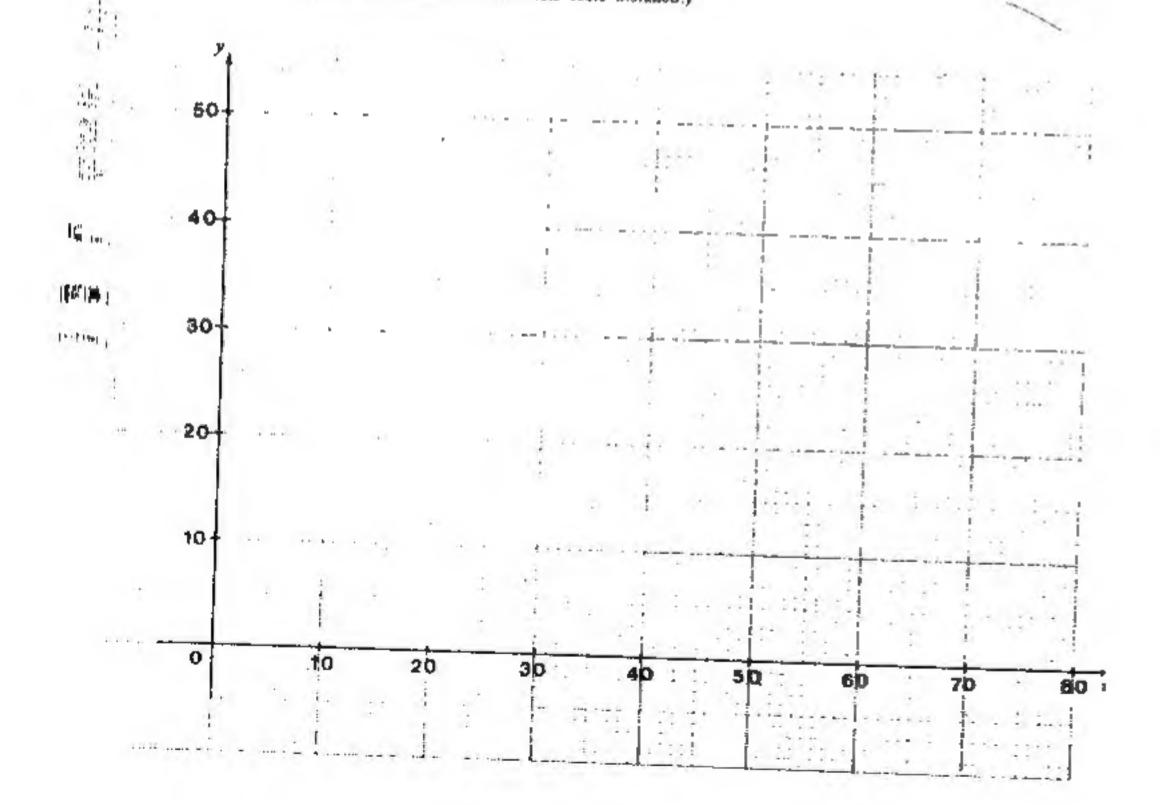
12. If you attempt this question, filt in the details in the first three boxes above and tie this sheet into your answer book.

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An airline company has a small passenger plane with a luggage capacity of 720 kg, and a floor area of 60 m<sup>2</sup> for installing passenger seats. An economy-class seat takes up 1 m<sup>2</sup> of floor area while a first-class seat takes up 1.5 m<sup>2</sup>. The company requires that the number of first-class seats should not exceed the number of economy-class newts. An economy-class passenger cannot carry more than 10 kg of luggage while a first-class passenger cannot carry more than 30 kg of luggage.

The profit from selling a first-class ticket is double that from selling an economy-class ticket. If all tickets are sold out in every flight, find graphically how many aconomy-class seats and how many first-class seats should be installed to give the company the maximum profit.

(Let x be the number of economy-class seats installed,
y be the number of first-class seats installed.)



13. (a) It is given that  $f(x) = 2x^2 + ax + b$ .

- If f(x) is divided by (x 1), the remainder is -5. If f(x) is divided by (x + 2), the remainder is 4. Find the values of a and b.
- (ii) If f(x) = 0, find the value of x.

(6 marks)

(b) Solve the equation

$$1 - 2x = \sqrt{2 - x}$$

Check to see whether the solutions satisfy the equation.

(4 marks)

14.

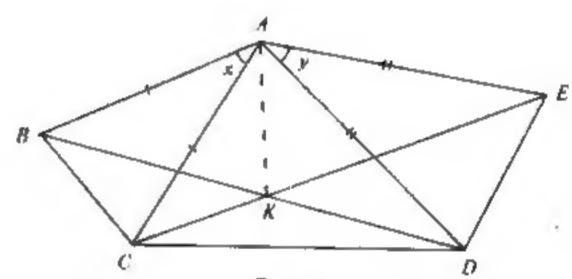


Figure 6

In Figure 6, AB = AC, AD = AE, Lx = Ly Straight lines BD and CE intersect at K.

(a) Prove that ΔABD and ΔACE are congruent.

(5 marks)

(b) Prove that ABCK is a cyclic quadrilateral.

(3 marks)

(c) Besides the quadrilateral ABCK, there is another cyclic quadrilateral in the figure. Write it down (proof is not required).

(2 marks)

15. In  $\triangle ABC$  (see Figure 7),  $BD = \frac{1}{4}AB$ .  $CE = \frac{1}{3}AC$ , BE intersects CD at P. Lx = Ly.

Prove that

- (a)  $\triangle EMC$  and  $\triangle ADC$  are similar / and  $EM = \frac{1}{4}AB$ , (4 marks)
- (b) ΔBDP and ΔEMP are congruent,

(2 marks)

- (c) PM = CM. (2 marks)
- (d) area of triangle BDP is half the area of triangle PEC.

  (2 marks)

Figure 7

CI Water ....

- It is given that  $f(x) = 2x^2 + ax + b$ . 13. (a)
  - If f(x) is divided by (x 1), the remainder is -5If f(x) is divided by  $\{x + 2\}$ , the remainder is 4 Find the values of a and b.
  - If f(x) = 0, find the value of x.

(6 marks)

Solve the equation

$$1-2x=\sqrt{2-x}$$

Check to see whether the solutions satisfy the equation,

(4 marks)

The examination for a professional qualification consists of a theory paper and a practical paper To obtain the qualification, a candidate has to pass both papers. If a candidate fails in either paper, he need only sit that paper again,

The probabilities of passing the theory paper for two candidates A and B are both  $\frac{4}{10}$  and their probabilities of passing the practical paper are both  $\frac{2}{3}$ . Find the probabilities of the following events:

Candidate A obtaining the qualification by sitting each paper only once.

(3 marks)

Candidate A failing in one of the two papers but obtaining the qualification (b) with one re-examination.

(4 marks)

At least one of the candidates A and B obtaining the qualification without (c) any re-examination.

(3 marks)

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15. The circle

$$x^2 + y^2 - 10x + 8y + 16 = 0$$

cuts the x-axis at A and B and touches the y-axis at T as shown in Figure 6.

- Find the coordinates of A, B and T. (5 marks)
- C is a point on the circle such that AC | TB
  - Find the equation of AC.

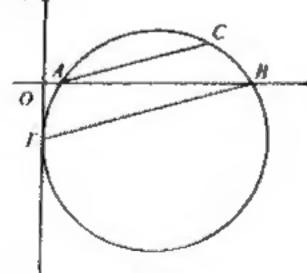
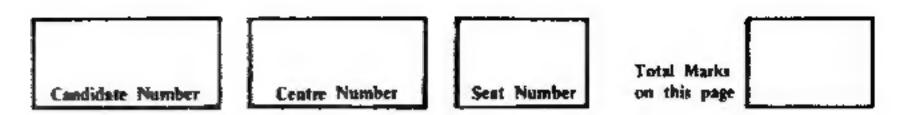


Figure 6

Find the coordinates of C by solving simultaneously the equation of AC and (11) the equation of the given circle.

(5 marks)



If you attempt this question, (ii) in the details in the first three boxes above and tie this sheet into your answer book.

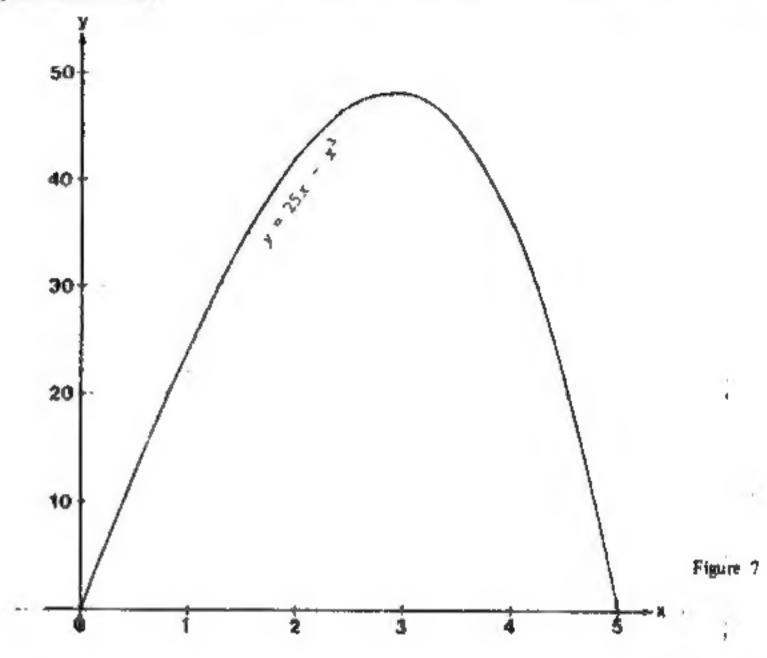


Figure 7 shows the graph of  $y = 25x - x^3$  for  $0 \le x \le 5$ . By adding a suitable straight line to the graph, solve the equation

$$30 = 25x - x^3,$$

where  $0 \le x \le 5$ . Give your answers correct to 2 significant figures.

(2 marks)

Figure 1 shows a right pyramid with a square base ABCD. AB = b units and AE = 5 units. The height of the pyramid is h units and its volume is V cubic units.

(i) Express b in terms of h. Hence show that  $V = \frac{2}{3}(25h - h^3)$ . (3 marks)

Using (2), find the two values of h such that V = 20. (Your answers should be correct to 2 significant figures.)

(2 marks)

Use the "method of magnification" to find the smaller value of h in (b) (ii) correct to 3 significant figures. (3 marks) Figure 8

END OF PAPER